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Hypergeometric Transformations Involving Terminating Clausen's Series Using Beta Integral Technique

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Abstract: The main object of this paper is to obtain the correct form of two erroneous integrals of Erdélyi et al. [Tables of Integral Transforms, Vol.II, p.284(16.4.1 and 16.4.3)]. Five hypergeometric transformations of the terminating Clausen's series ${}_3F_2$ are also obtained.

Keywords and Phrases: Jacobi Polynomials, Clausen's series, Saalsch \ddot{u} tz' theorem, Gauss's theorem.

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1 Introduction and Preliminaries

Throughout in the present paper, we use the following standard notations:

$$\mathbb{N} := \{1, 2, 3, \ldots\}, \, \mathbb{N}_0 := \{0, 1, 2, 3, \ldots\} = \mathbb{N} \cup \{0\} \text{ and } \mathbb{Z}^- := \{-1, -2, -3, \ldots\} = \mathbb{Z}_0^- \setminus \{0\}.$$

Here, as usual, \mathbb{Z} denotes the set of integers, \mathbb{R} denotes the set of real numbers, \mathbb{R}^+ denotes the set of positive real numbers and \mathbb{C} denotes the set of complex numbers.

The Pochhammer symbol (or the shifted factorial) $(\lambda)_{\nu}$ $(\lambda, \nu \in \mathbb{C})$ is defined, in terms of the familiar Gamma function, by

$$(\lambda)_{\nu} := \frac{\Gamma(\lambda + \nu)}{\Gamma(\lambda)} = \begin{cases} 1 & (\nu = 0; \lambda \in \mathbb{C} \setminus \{0\}) \\ \lambda(\lambda + 1) \dots (\lambda + n - 1) & (\nu = n \in \mathbb{N}; \lambda \in \mathbb{C}) \end{cases}$$
(1.1)

it being understood *conventionally* that $(0)_0 = 1$ and assumed tacitly that the Gamma quotient exists.

In the Gaussian hypergeometric series ${}_{2}F_{1}(a,b;c;z)$ there are two numerator parameters a,b and one denominator parameter c. A natural generalization of this series is accomplished by introducing any arbitrary number of numerator and denominator parameters. The resulting series